



# Key Establishment Schemes Workshop Document

October 2001



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## Introduction

- ◆ Many cryptographic algorithms (e.g., AES, HMAC) require the establishment of *shared keying material* in advance.
- ◆ Manual distribution of keying material is inefficient and complex.
- ◆ Seek automated key establishment schemes.



## Scope & Purpose

- ◆ Development of a Federal key agreement schemes document based on
  - **ANSI X9.42** Agreement of Symmetric Keys using Discrete Logarithm Cryptography
  - **ANSI X9.44** Key Agreement and Key Transport using Factoring-Based Cryptography (To be provided)
  - **ANSI X9.63** Key Agreement and Key Transport using Elliptic Curve Cryptography



## Definitions

- ◆ Approved
  - FIPS approved or NIST Recommended
- ◆ Keying Material
  - The data (e.g., keys and IVs) necessary to establish and maintain cryptographic keying relationships.
- ◆ Shared Keying Material
  - The keying material that is derived by applying a key derivation function to the shared secret.
- ◆ Shared Secret
  - A secret value computed using a prescribed algorithm and combination of keys belonging to the participants in the key establishment scheme.



## General Symbols

H	An approved hash function
$[Text_1], [Text_2]$	An optional bit string that may be used during key confirmation and that is sent between the parties establishing keying material
U	One entity of a key establishment process, or the bit string denoting the identity of that entity
V	The other entity of a key establishment process, or the bit string denoting the identity of that entity
$X  Y$	Concatenation of two strings $X$ and $Y$



## ANSI X9.42 Symbols

$p, q, g$	The domain parameters
$\text{mod } p$	The reduction modulo $p$ on an integer value
$r_U, r_V$	Party U or Party V's ephemeral private key
$t_U, t_V$	Party U or Party V's ephemeral public key
$x_U, x_V$	Party U or Party V's static private key
$y_U, y_V$	Party U or Party V's static public key
$Z$	A shared secret that is used to derive keying material using a key derivation function
$Z_e$	An ephemeral shared secret that is computed using the Diffie-Hellman primitive
$Z_s$	A static shared secret that is computed using the Diffie-Hellman primitive



## ANSI X9.63 Symbols

$[X]$	Indicates that the inclusion of the bit string or octet string $X$ is optional
$a, b$	Field elements that define the equation of an elliptic curve
$avf(P)$	The associate value of the elliptic curve point
$d_{e,U}, d_{e,V}$	Party U's and Party V's ephemeral private keys
$d_{s,U}, d_{s,V}$	Party U's and Party V's static private keys
$FR$	An indication of the basis used
$G$	A distinguished point on an elliptic curve
$h$	The cofactor of the elliptic curve



## ANSI X9.63 Symbols

$n$	The order of the point $G$
$q$	The field size
$j$	A special point on an elliptic curve, called the point at infinity. The additive identity of the elliptic curve group.
$Q_{e,U}, Q_{e,V}$	Party U's and Party V's ephemeral public keys
$Q_{s,U}, Q_{s,V}$	Party U's and Party V's static public keys
$SEED$	An optional bit string that is present if the elliptic curve was randomly generated
$x_P$	The $x$ -coordinate of a point $P$ .
$y_P$	The $y$ -coordinate of a point $P$ .
$Z$	A shared secret that is used to derive key using a key derivation function
$Z_e$	An ephemeral shared secret that is computed using the Diffie-Hellman primitive
$Z_s$	A static shared secret that is computed using the Diffie-Hellman primitive



## Key Establishment Algorithm Classes

- ◆ Cryptographic keying material may be electronically established between parties using either key agreement or key transport schemes.
- ◆ During key agreement, the keying material to be established is not sent; information is exchanged between the parties that allow the calculation of the keying material. Key agreement schemes use asymmetric (public key) techniques.
- ◆ During key transport, encrypted keying material is sent from an initiator who generates the keying material to another party. Key transport schemes use either symmetric or public key techniques.



## Security Attributes

- ◆ To be determined...



## Cryptographic Elements

- ◆ Domain Parameters (Generation, Validation, and Management)
- ◆ Private/Public Keys (Generation, PK Validation, Management)
- ◆ Key Derivation Function
- ◆ Message Authentication Code
- ◆ Associate Value Function (Elliptic Curves Only)
- ◆ Cryptographic Hash Functions
- ◆ Random Number Generation
- ◆ Key Confirmation
- ◆ Calculation of Shared Secrets
- ◆ RSA Primitives (To be provided)
- ◆ Key Wrapping Primitive(s) (To be provided)



## Domain Parameter Generation

### ◆ ANSI X9.42 Requirements

- $(p, q, g)$  where  $p$  and  $q$  are prime, and  $g$  is the generator of the  $q$ -order cyclic subgroup of  $GF(p)$

### ◆ ANSI X9.63 Requirements

- $(q, FR, a, b, [SEED], G, n, h)$  where  $q$  (field size),  $FR$  (basis used),  $a$  and  $b$  (field elements),  $SEED$  (optional bit string),  $G$  (point),  $n$  (order of the point  $G$ ), and  $h$  (cofactor).



## Domain Parameter Validation

### ◆ One of three methods must be employed before use

- The party generates (and checks) the parameters
- The party validates parameters as specified in appropriate ANSI standards
- The party receives assurance from a trusted party (e.g., a CA) that the parameters are valid by one of the above methods



## Domain Parameter Management

- ◆ Only authorized (trusted) parties should generate domain parameters
- ◆ Key pairs must be associated with their domain parameters
- ◆ Modification or substitution of domain parameters may cause security risks



## Private/Public Keys

- ◆ Key Pair Generation
  - Static and ephemeral key pairs are generated using the same primitives
  - Private keys must be created using an approved RNG
- ◆ Public Key Validation
  - Static public keys **must** be validated by the recipient, or by an entity that is trusted by the recipient
  - Each ephemeral public key **must** be validated by the recipient before being used to derive a shared secret
- ◆ Key Pair Management
  - Public/private key pairs **must** be correctly associated with their corresponding domain parameters
  - Static public keys **must** be obtained in a trusted manner
  - Ephemeral keys **must** be destroyed immediately after the shared secret is computed





## Cryptographic Elements

- ◆ Key Derivation Function (KDF)
  - Used to derive keying material from a shared secret
  - Uses identities of communicating parties
- ◆ Message Authentication Code (MAC)
  - A function of both a symmetric key and data
  - MAC function used to provide key confirmation
- ◆ Associate Value Function (EC Only)
  - Used by the MQV family of key agreement schemes to compute an integer associated with an elliptic curve point



## Cryptographic Elements

- ◆ Cryptographic Hash Functions
  - Use approved hash functions whenever required.
- ◆ Random Number Generation
  - Use approved random number generators whenever required
- ◆ Key Confirmation
  - Used to provide assurance that the parties have derived the same keys



## Calculation of Shared Secrets

- ◆ Use DH of ANSI X9.42 for dhHybrid1, dhEphem, dhHybridOneFlow, dhOneFlow, and dhStatic schemes
- ◆ Use Modified DH of ANSI X9.63 for Full Unified Model, Ephemeral Unified Model, 1-Pass Unified Model, 1-Pass Diffie-Hellman, and Static Unified Model Schemes (Differs from ANSI X9.63)



## Calculation of Shared Secrets

- ◆ Use MQV2 primitive of ANSI X9.42 for the MQV2 scheme
- ◆ Use MQV1 primitive of ANSI X9.42 for MQV1 scheme
- ◆ Use MQV primitive of Section 5.5 of ANSI X9.63 for Full MQV and 1-Pass MQV schemes
- ◆ Shared Secrets
  - **must not** be used directly as shared keying material.
  - **must** be calculated by applying a key derivation function to the shared secret.



## Other Primitives

- ◆ RSA Primitives
  - To be addressed later...
- ◆ Key Wrapping Primitive(s)
  - To be addressed later...



## Key Agreement Schemes Categories

- ◆ **C(2): Two Party Participation**
  - *Interactive, 2-way*
  - Each party generates an ephemeral key pair.
- ◆ **C(1): One Party Participation**
  - *Store-and-Forward, 1-way*
  - Only the initiator generates an ephemeral key pair.
- ◆ **C(0): Static Keys Only**
  - *Static (passive)*
  - No ephemeral keys are used.



## Key Agreement Schemes Subcategories

- ◆ C(2,2): Each party generates an ephemeral key pair and has a static key pair.
- ◆ C(2,0): Each party generates an ephemeral key pair; no static keys are used.
- ◆ C(1,2): The initiator generates an ephemeral key pair and has a static key pair; the responder has a static key pair.
- ◆ C(1,1): The initiator generates an ephemeral key pair, but has no static key pair; the responder has only a static key pair.
- ◆ C(0,2): Each party has only static keys.



## Key Agreement Schemes Subcategories

- ◆ Primitive: Either a DH or an MQV primitive
- ◆ Arithmetic: Either FF as in ANSI X9.42 or EC as in ANSI X9.63
- ◆ Example: dhHybrid1 can be classified as C(2, 2, DH, FF)



## Key Agreement Schemes

Category	Subcategory	Primitive	Arith.	Scheme	Full Classification
$C(2)$	$C(2,2)$	DH	FF	dhHybrid1	$C(2,2,DH,FF)$
$C(2)$	$C(2,2)$	DH	EC	Full Unified Model	$C(2,2,DH,EC)$
$C(2)$	$C(2,2)$	MQV	FF	MQV2	$C(2,2,MQV,FF)$
$C(2)$	$C(2,2)$	MQV	EC	Full MQV	$C(2,2,MQV,EC)$
$C(2)$	$C(2,0)$	DH	FF	dhEphem	$C(2,0,DH,FF)$
$C(2)$	$C(2,0)$	DH	EC	Ephemeral Unified Model	$C(2,0,DH,EC)$
$C(1)$	$C(1,2)$	DH	FF	dhHybridOneFlow	$C(1,2,DH,FF)$
$C(1)$	$C(1,2)$	DH	EC	1-Pass Unified Model	$C(1,2,DH,EC)$
$C(1)$	$C(1,2)$	MQV	FF	MQV1	$C(1,2,MQV,FF)$
$C(1)$	$C(1,2)$	MQV	EC	1-Pass MQV	$C(1,2,MQV,EC)$
$C(1)$	$C(1,1)$	DH	FF	dhOneFlow	$C(1,1,DH,FF)$
$C(1)$	$C(1,1)$	DH	EC	1-Pass Diffie-Hellman	$C(1,1,DH,EC)$
$C(0)$	$C(0,2)$	DH	FF	dhStatic	$C(0,2,DH,FF)$
$C(0)$	$C(0,2)$	DH	EC	Static Unified Model	$C(0,2,DH,EC)$



## Key Agreement Schemes Overview

- ◆ Each party in a key agreement process **must** use the same domain parameters.
- ◆ These parameters **must** be established prior to the initiation of the key agreement process.
- ◆ Static public keys may be obtained from other entity or trusted third party (e.g., a CA)

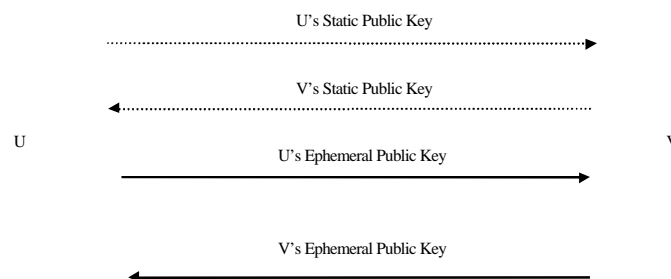


## Two Party Participation C(2)

- ◆ Each party generates an ephemeral key pair and has a static key pair
- ◆ *Four* C(2,2) schemes
  - dhHybrid1
  - Full Unified Model
  - MQV2
  - Full MQV



**Figure 1: General Protocol when each party has both static and ephemeral key pairs**



1. U uses its static and ephemeral private keys and V's static and ephemeral public keys to compute a shared secret.
2. U invokes the Key Derivation Function using the shared secret.

1. V uses its static and ephemeral private keys and U's static and ephemeral public keys to compute a shared secret.
2. V invokes the Key Derivation Function using the shared secret.



**Table 4: dhHybrid1 Key Agreement Scheme C(2,2,DH,FF)**

	<b>Party U</b>	<b>Party V</b>
<b>Static Data</b>	1. Static private key $x_U$ 2. Static public key $y_U$	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	1. Ephemeral private key $r_V$ 2. Ephemeral public key $t_V$
<b>Input</b>	$(p, q, g), x_U, y_U, r_U, t_U$	$(p, q, g), x_V, y_V, r_V, t_V$
<b>Computation</b>	$Z_s = y_V^{x_U} \bmod p$ $Z_e = t_V^{r_U} \bmod p$	$Z_s = y_U^{x_V} \bmod p$ $Z_e = t_U^{r_V} \bmod p$
<b>Derive Key Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$



**Table 5: Full Unified Model Key Agreement Scheme C(2,2,DH,EC)**

	<b>Party U</b>	<b>Party V</b>
<b>Static Data</b>	1. Static private key $d_{s,U}$ 2. Static public key $Q_{s,U}$	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	1. Ephemeral private key $d_{e,V}$ 2. Ephemeral public key $Q_{e,V}$
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{e,U}, Q_{e,U}, d_{s,U}, Q_{s,U}$	$(q, FR, a, b, [SEED], G, n, h), d_{e,V}, Q_{e,V}, d_{s,V}, Q_{s,V}$
<b>Computation</b>	$(x_s, y_s) = hd_{s,U}(Q_{s,V})$ $(x_e, y_e) = hd_{e,U}(Q_{e,V})$ $Z_s = x_s$ $Z_e = x_e$	$(x_s, y_s) = hd_{s,V}(Q_{s,U})$ $(x_e, y_e) = hd_{e,V}(Q_{e,U})$ $Z_s = x_s$ $Z_e = x_e$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$



**Table 6: MQV2 Key Agreement Scheme C(2,2,MQV,FF)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $x_U$ 2. Static public key $y_U$	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	1. Ephemeral private key $r_V$ 2. Ephemeral public key $t_V$
<b>Input</b>	$(p, q, g), x_U, y_U, r_U, t_U, t_V$	$(p, q, g), x_V, y_V, r_V, t_V, t_U$
<b>Computation</b>	1. $w = \lceil \ q\ /2 \rceil$ 2. $t_U \epsilon = (t_U \bmod 2^w) + 2^w$ 3. $S_U = (r_U + t_U \epsilon x_U) \bmod q$ 4. $t_V \epsilon = (t_V \bmod 2^w) + 2^w$ 5. $Z_{MQV} = (t_V y_V^{t_U \epsilon})^{S_U} \bmod p$	1. $w = \lceil \ q\ /2 \rceil$ 2. $t_V \epsilon = (t_V \bmod 2^w) + 2^w$ 3. $S_V$  $Z_{MQV} = (t_U y_U^{t_V \epsilon})^{S_V} \bmod p.$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_{MQV}$	Compute $kdf(Z, OtherInput)$ using $Z = Z_{MQV}$



**Table 7: Full MQV Key Agreement Scheme C(2,2,MQV,EC)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $d_{s,U}$ 2. Static public key $Q_{s,U}$	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	1. Ephemeral private key $d_{e,V}$ 2. Ephemeral public key $Q_{e,V}$
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{e,U}, Q_{e,U}, d_{s,U}, Q_{e,U}, Q_{s,V}$	$(q, FR, a, b, [SEED], G, n, h), d_{e,V}, Q_{e,V}, d_{s,V}, Q_{e,V}, Q_{s,U}$
<b>Computation</b>	1. $implicit_{sig}_U = (d_{e,U} + \text{avf}(Q_{e,U})d_{s,U}) \bmod n$ 2. $(x, y) = h \times implicit_{sig}_U \times (Q_{e,V} + \text{avf}(Q_{e,V})Q_{s,V})$ 3. $Z = x$	1. $implicit_{sig}_V = (d_{e,V} + \text{avf}(Q_{e,V})d_{s,V}) \bmod n$ 2. $(x, y) = h \times implicit_{sig}_V \times (Q_{e,U} + \text{avf}(Q_{e,U})Q_{s,U})$ 3. $Z = x$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = x$	Compute $kdf(Z, OtherInput)$ using $Z = x$



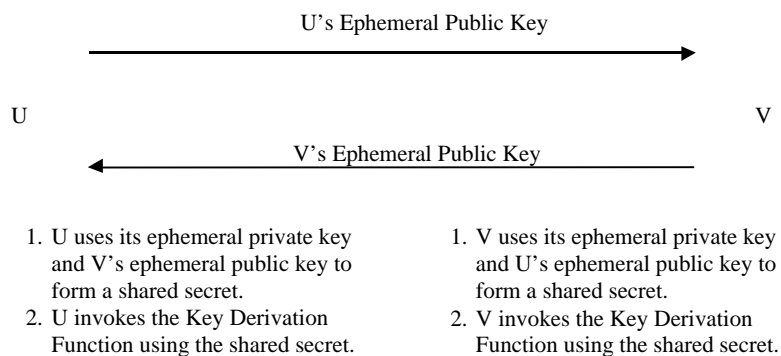


## Two Party Participation

- ◆ Each party generates an ephemeral key pair; no static keys are used.
- ◆ *Two*  $C(2,0)$  schemes
  - dhEphem
  - Ephemeral Unified Model



**Figure 2: General protocol when each party generates ephemeral key pairs; no static keys are used**





**Table 8: dhEphem Key Agreement Scheme C(2,0,DH,FF)**

	Party U	Party V
<b>Static Data</b>	N/A	N/A
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	1. Ephemeral private key $r_V$ 2. Ephemeral public key $t_V$
<b>Input</b>	$(p, q, g), r_U, t_V$	$(p, q, g), r_V, t_U$
<b>Computation</b>	$Z_e = t_V^{r_U} \bmod p$	$Z_e = t_U^{r_V} \bmod p$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$



**Table 9: Ephemeral Unified Model Key Agreement Scheme C(2,0,DH,EC)**

	Party U	Party V
<b>Static Data</b>	N/A	N/A
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	1. Ephemeral private key $d_{e,V}$ 2. Ephemeral public key $Q_{e,V}$
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h),$ $d_{e,U}, Q_{e,V}$	$(q, FR, a, b, [SEED], G, n, h),$ $d_{e,V}, Q_{e,U}$
<b>Computation</b>	$(x_e, y_e) = hd_{e,U}(Q_{e,V})$ $Z_e = x_e$	$(x_e, y_e) = hd_{e,V}(Q_{e,U})$ $Z_e = x_e$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$

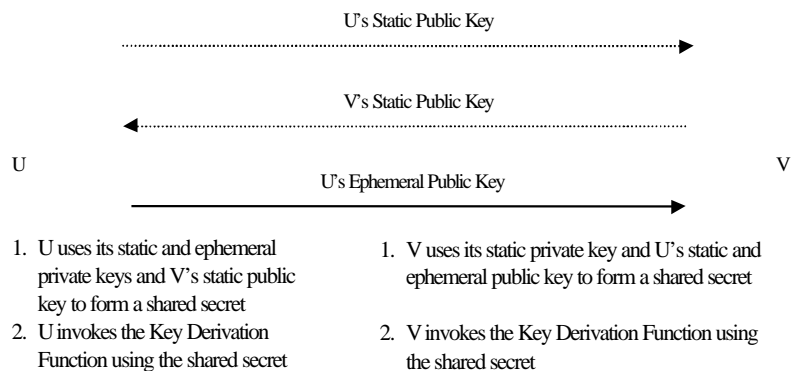


## One Party Participation

- ◆ Initiator has a static key pair and generates an ephemeral key pair; Responder has a static key pair.
- ◆ *Four* C(1,2) schemes
  - dhHybridOneFlow
  - 1-Pass Unified Model
  - MQV1
  - 1-Pass MVQ



**Figure 3: General protocol when the Initiator has both static and ephemeral key pairs, and the Responder has only a static key pair**





**Table 10: dhHybridOneFlow Key Agreement Scheme C(1,2,DH,FF)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $x_U$ 2. Static public key $y_U$	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	N/A
<b>Input</b>	$(p, q, g), x_U, r_U, y_V$	$(p, q, g), x_V, y_U, t_U$
<b>Computation</b>	$Z_s = y_V^{x_U} \bmod p$ $Z_e = y_V^{r_U} \bmod p$	$Z_s = y_U^{x_V} \bmod p$ $Z_e = t_U^{x_V} \bmod p$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$



**Table 11: 1-Pass Unified Model Key Agreement Scheme C(1,2,DH,EC)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $d_{s,U}$ 2. Static public key $Q_{s,U}$	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	N/A
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{s,U}, d_{e,U}, Q_{s,V}$	$(q, FR, a, b, [SEED], G, n, h), d_{s,V}, Q_{s,U}, Q_{e,U}$
<b>Computation</b>	$(x_s, y_s) = h d_{s,U} Q_{s,V}$ $(x_e, y_e) = h d_{e,U} Q_{s,V}$ $Z_s = x_s$ $Z_e = x_e$	$(x_s, y_s) = h d_{s,V} Q_{s,U}$ $(x_e, y_e) = h d_{s,V} Q_{e,U}$ $Z_s = x_s$ $Z_e = x_e$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e    Z_s$



**Table 12: MQV1 Key Agreement Scheme C(1,2,MQV,FF)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $x_U$ 2. Static public key $y_U$	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	N/A
<b>Input</b>	$(p, q, g), x_U, y_U, r_U, t_U$	$(p, q, g), x_V, y_V, t_V$
<b>Computation</b>	1. $w = \lceil \ q\ /2 \rceil$ 2. $t_U' = (t_U \bmod 2^w) + 2^w$ 3. $S_U = (r_U + t_U' x_U) \bmod q$ 4. $y_V' = (y_V \bmod 2^w) + 2^w$ 5. $Z_{MQV} = (y_V y_V'^{y_V^{-1}})^{S_U} \bmod p$	1. $w = \lceil \ q\ /2 \rceil$ 2. $y_V' = (y_V \bmod 2^w) + 2^w$ 3. $S_V = (x_V + y_V' x_V) \bmod q$ 4. $t_U' = (t_U \bmod 2^w) + 2^w$ 5. $Z_{MQV} = (t_U y_U^{t_U^{-1}})^{S_V} \bmod p$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_{MQV}$	Compute $kdf(Z, OtherInput)$ using $Z = Z_{MQV}$

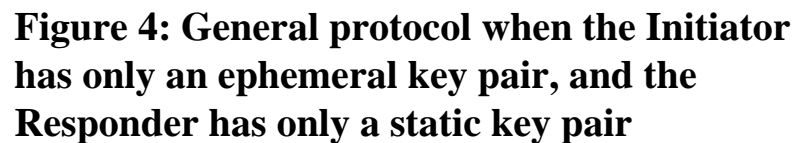


**Table 13:1-Pass MQV Model Key Agreement Scheme C(1,2,MQV,EC)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $d_{s,U}$ 2. Static public key $Q_{s,U}$	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	N/A
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{e,U}, d_{s,U}, Q_{e,U}, Q_{s,U}$	$(q, FR, a, b, [SEED], G, n, h), d_{s,V}, Q_{s,V}, Q_{e,U}, Q_{s,U}$
<b>Computation</b>	1. $implicit_{sig_U} = (d_{e,U} + avf(Q_{e,U})d_{s,U}) \bmod n$ 2. $(x, y) = h \times implicit_{sig_U} \times (Q_{s,V} + avf(Q_{s,V})Q_{s,V})$ 3. $Z = x$	1. $implicit_{sig_V} = (d_{s,V} + avf(Q_{s,V})d_{s,V}) \bmod n$ 2. $(x, y) = h \times implicit_{sig_V} \times (Q_{e,U} + avf(Q_{e,U})Q_{s,U})$ 3. $Z = x$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = x$	Compute $kdf(Z, OtherInput)$ using $Z = x$



- ## One Party Participation





**Table 14: dhOneFlow Key Agreement Scheme C(1,1,DH,FF)**

	Party U	Party V
<b>Static Data</b>	N/A	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	1. Ephemeral private key $r_U$ 2. Ephemeral public key $t_U$	N/A
<b>Input</b>	$(p, q, g), r_U, y_V$	$(p, q, g), x_V, t_U$
<b>Computation</b>	$Z_e = y_V^{r_U} \bmod p$	$Z_e = t_U^{x_V} \bmod p$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$	Compute $kdf(Z, OtherInput)$ using $Z = Z_e$



**Table 15: 1-Pass Diffie-Hellman Model Key Agreement Scheme C(1,1,DH,EC)**

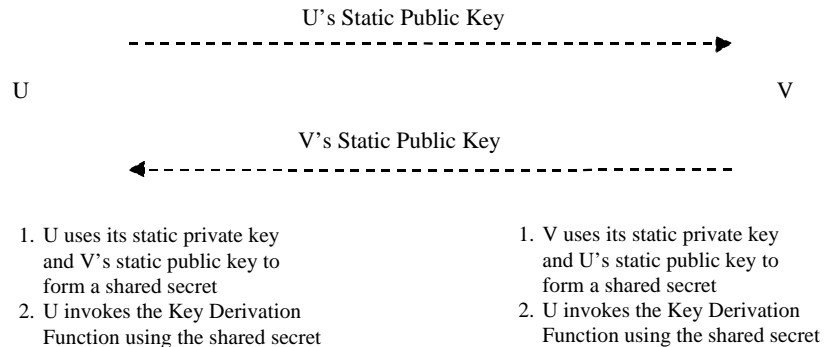
	Party U	Party V
<b>Static Data</b>	N/A	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	1. Ephemeral private key $d_{e,U}$ 2. Ephemeral public key $Q_{e,U}$	N/A
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{e,U}, Q_{s,V}$	$(q, FR, a, b, [SEED], G, n, h), d_{s,V}, Q_{e,U}$
<b>Computation</b>	$(x, y) = h d_{e,U} Q_{s,V}$  $Z = x$	$(x, y) = h d_{s,V} Q_{e,U}$  $Z = x$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = x$	Compute $kdf(Z, OtherInput)$ using $Z = x$



## Static Keys Only

- ◆ Each party has only a static key pair
- ◆ Two C(0,2) schemes
  - dhStatic
  - Static Unified Model

### Figure 5: Each party has only a static key pair







**Table 16: dhStatic Key Agreement Scheme C(0,2,DH,FF)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $x_U$ 2. Static public key $y_U$	1. Static private key $x_V$ 2. Static public key $y_V$
<b>Ephemeral Data</b>	N/A	N/A
<b>Input</b>	$(p, q, g), x_U, y_V$	$(p, q, g), x_V, y_U$
<b>Computation</b>	$Z_s = y_V^{x_U} \bmod \phi$	$Z_s = y_U^{x_V} \bmod \phi$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_s$



**Table 17: Static Unified Model Key Agreement Scheme C(0,2,DH,EC)**

	Party U	Party V
<b>Static Data</b>	1. Static private key $d_{s,U}$ 2. Static public key $Q_{s,U}$	1. Static private key $d_{s,V}$ 2. Static public key $Q_{s,V}$
<b>Ephemeral Data</b>	N/A	N/A
<b>Input</b>	$(q, FR, a, b, [SEED], G, n, h), d_{s,U}, Q_{s,V}$	$(q, FR, a, b, [SEED], G, n, h), d_{s,V}, Q_{s,U}$
<b>Computation</b>	$(x_s, y_s) = hd_{s,U}Q_{s,V}$ $Z_s = x_s$	$(x_s, y_s) = hd_{s,V}Q_{s,U}$ $Z_s = x_s$
<b>Derive Keying Material</b>	Compute $kdf(Z, OtherInput)$ using $Z = Z_s$	Compute $kdf(Z, OtherInput)$ using $Z = Z_s$



## Topics to be Addressed

- ◆ Key Transport
  - To be addressed
- ◆ Keys Derived from a “Master Key”
  - Suggestions welcome



## Key Recovery

- ◆ Some applications may desire to recover protected data by first recovering the associated key
- ◆ Static key pairs may be saved (See Key Management Guideline document)
- ◆ Static public keys may be saved (e.g., public key certificates)
- ◆ Ephemeral public keys may be saved
- ◆ Ephemeral private keys **must not** be recoverable or saved

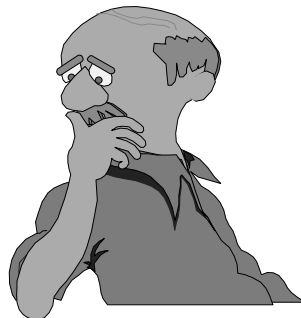


## Implementation Validation

- ◆ Implementations of schemes in the final schemes document must be tested in order to claim compliance
- ◆ For information on NIST's testing program see <http://csrc.nist.gov/cryptval>



## Questions?





Give me a break!



## Discussion Topics

- ◆ Are there any situations which are not addressed by at least one of the schemes in the document?
- ◆ Which schemes should use key confirmation?
- ◆ Should key confirmation ever be mandatory?
- ◆ Does it unnecessarily hinder any application to require a distinction between initiator and responder in a scheme?
- ◆ Should the identities of the initiator and responder be used in the calculation of shared secrets? (related to previous question)

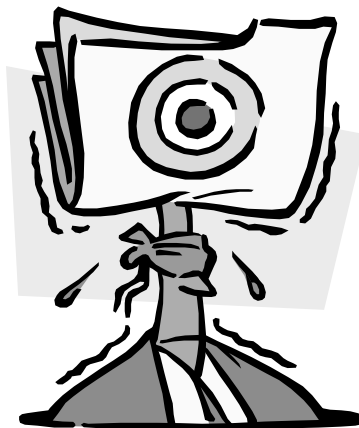


## Discussion Topics

- ◆ Should this document address broader forms of key derivation (e.g., key derivation for multi-user applications)?
- ◆ What are the most important key establishment scheme attributes, and how should they be presented? (Please bring your ideas)
- ◆ Are there any additional topics that should be covered?
- ◆ Are there any additional appendices that should be included?



## Questions or Discussion?





## Closing

- ◆ Thanks for coming and helping
- ◆ See <http://www.nist.gov/kms>
- ◆ We will let you know when report is posted
- ◆ Send comments to [kmscomments@nist.gov](mailto:kmscomments@nist.gov)
- ◆ Have a safe trip home